ALGEBRA 12

Description

This first course in algebra furthers the students' skills in operating with real numbers, variables and algebraic properties. Algebra 12 also develops the concept of function. Major topics include: number properties, operations with real numbers, solutions of linear and quadratic equations, graphing functions, data analysis, radicals, exponents, factoring, solutions of systems of linear equations. Throughout the course, there will be an integration of problem solving techniques, communication skills, computing and estimating, the use of technology, and real life applications.

Course Overview					
Course Goals	Essential Questions	Assessments			
Students should:	• How do patterns and functions help us describe data and physical phenomena and solve a variety of problems?	Common Assessments			
	 How are quantitative relationships represented by numbers? How can collecting, organizing and displaying data help us analyze information and make reasonable predictions and informed decisions? 	Skill Assessments			
Content Outline	Standards	Grade Level Skills			
I. Unit 1 - Foundations of Algebra		Students will:			
II. <u>Unit 2</u> - Algebraic Expressions and Equations	State of Connecticut Math Curriculum Frameworks	Skills Matrix			
III. Unit 3 - Functions and Relations	Connecticut State Standards are met in the				
IV. Unit 4 - Graphing	following areas:				
V. <u>Unit 5</u> - Exponents and Radicals VI. Unit 6 Polynomials	 Algebraic Reasoning: Patterns And Functions Numerical and Proportional Reasoning Working with Data: Probability and Statistics 				

Pacing Guide									
1st Ma	Iarking Period 2nd Marking Period			3rd Marking Period			4th Marking Period		
September	October Nove	ember D	December	January	February	March	April	May	June
Unit 1	Unit 2		U	nit 3	Uı	nit 4	U	nit 5	Unit 6
<u>Foundations</u> <u>of Algebra</u>	Algebraic Express Equations	ions and	<u>Funct</u> <u>Rel</u>	<u>ions and</u> ations	Gra	phing	Expor Ra	<u>ents and</u> dicals	<u>Polynomials</u>
2 weeks	7 weeks		6 v	veeks	7 ½	weeks	6 1	weeks	3 ¹ ⁄2 weeks

Unit 1 - Foundations of Algebra, 2 weeks top

<u>Standards</u>

Algebraic Reasoning: Patterns and Functions - Patterns and functional relationships can be represented and analyzed using a variety of strategies, tools, and technology.

1.1 Students should understand and describe patterns and functional relationships.

Core 1.1a Students should describe relationships and make generalizations about patterns and functions.

Extended 1.1a Students should model real world situations and make generalizations about mathematical relationships using a variety of patterns and functions.

Numerical and Proportional Reasoning - Quantitative relationships can be expressed numerically in multiple ways in order to make connections and simplify calculations using a variety of strategies, tools and technology.

2.1 Students should understand that a variety of numerical representations can be used to describe quantitative relationships.

- Core 2.1a Students should extend the understanding of number to include integers, rational numbers, and real numbers.
 - 2.1b Students should interpret and represent large sets of numbers with the aid of technology.

2.2 Students should use numbers and their properties to compute flexibly and fluently, and to reasonably estimate measures and quantities.

Core 2.2a Students should develop strategies for computation and estimation using properties of number systems to solve problems.

Working with Data: Probability and Statistics - Data can be analyzed to make informed decisions using a variety of strategies, tools and technology. 4.1 Students should collect, organize and display data using appropriate statistical and graphical methods.

Core 4.1a Students should create the appropriate visual or graphical representation of real data.

4.2 Students should analyze data sets to form hypotheses and make predictions.

Core 4.2a Students should analyze real world problems using statistical techniques.

Unit Objectives	Essential Questions	Assessment
 Students will be able to: collect, analyze, interpret and display data and statistics both manually and with 	• How do patterns and functions help us describe data and physical phenomena and solve a variety of problems?	Amazing Algebra Amusement Park Adventure
 technology. write and evaluate expressions compute using the order of operations use algebraic models to represent real-life situations organize data and represent functions 	 How are quantitative relationships represented by numbers? How can collecting, organizing and displaying data help us analyze information and make reasonable predictions and informed decisions? Focus Questions What is algebra and what role does it play in the world of mathematics? (i.e. Its importance as a foundation and tool in higher mathematics and 	 Skill Objectives Students will: perform operations on the real numbers using fractions, decimals, percents, absolute value and exponents. apply the order of operations to evaluate an expression. graph numbers on a number line. manipulate and demonstrate the interconnection between fractions,

 the real world.) Given a real-world situation or set of data h can an algebraic model be created and appli How can the order of operations help to eva expressions? How can data be represented? 	decimals and percents. • find the mean, median and mode of data. uate
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Unit 2 – Algebraic Expressions and Equations, 7 weeks top

<u>Standards</u>

Algebraic Reasoning: Patterns and Functions - Patterns and functional relationships can be represented and analyzed using a variety of strategies, tools, and technology.

1.3 Students should use operations, properties, and algebraic symbols to determine equivalence and solve problems.

Core 1.3a Students should manipulate equations, inequalities, and functions to solve problems.

Numerical and Proportional Reasoning - Quantitative relationships can be expressed numerically in multiple ways in order to make connections and simplify calculations using a variety of strategies, tools and technology.

2.1 Students should understand that a variety of numerical representations can be used to describe quantitative relationships.

- Core 2.1a Students should extend the understanding of number to include integers, rational numbers, and real numbers.
- 2.1b Students should interpret and represent large sets of numbers with the aid of technology.

2.2 Students should use numbers and their properties to compute flexibly and fluently, and to reasonably estimate measures and quantities.

- Core 2.2a Students should develop strategies for computation and estimation using properties of number systems to solve problems.
 - 2.2b Students should solve proportional reasoning problems.

Working with Data: Probability and Statistics - Data can be analyzed to make informed decisions using a variety of strategies, tools and technology. 4.3 Students should understand and apply basic concepts of probability.

Core

re 4.3a Students should understand and apply the principles of probability in a variety of situations.

<u>Unit Objectives</u>	Essential Questions	Assessment
 Students will be able to: identify and apply properties of equality and algebraic axioms 	• How do patterns and functions help us describe data and physical phenomena and solve a variety of problems?	Fairfield Extra Curricular Budget Predictions
 solve algebraic equations and inequalities. compute with real numbers and apply their properties. solve equations and inequalities with real numbers. determine probability and odds of an event. graph on a number line. solve real –life problems using ratios and presents. 	 How are quantitative relationships represented by numbers? How can collecting, organizing and displaying data help us analyze information and make reasonable predictions and informed decisions? Focus Questions What is algebra and what role does it play in the world of mathematics? (i.e. Its importance as a foundation and tool in higher mathematics and the real world.) How can we employ technology to create and interpret models and enhance student learning? 	 Skill Objectives Students will: define and apply properties of algebra, including commutative, associative, distributive, identity, and inverse. define, simplify, and evaluate variable expressions and equations. solve proportions and use them to model real world problems. solve equations and inequalities with variables on one or both sides using one or more operations (including linear, absolute value, quadratic, exponential

Unit 3 - Functions and Relations, 6 weeks top

<u>Standards</u>

Algebraic Reasoning: Patterns and Functions - Patterns and functional relationships can be represented and analyzed using a variety of strategies, tools, and technology.

1.1 Students should understand and describe patterns and functional relationships.

Core 1.1a Students should describe relationships and make generalizations about patterns and functions.

Extended 1.1a Students should model real world situations and make generalizations about mathematical relationships using a variety of patterns and functions.

1.2 Students should represent and analyze quantitative relationships in a variety of ways.

Core 1.2a Students should represent and analyze linear and non-linear functions and relations symbolically and with tables and graphs.

1.3 Students should use operations, properties, and algebraic symbols to determine equivalence and solve problems.

Core 1.3a Students should manipulate equations, inequalities, and functions to solve problems.

Unit Objectives Students will be able to: • create, manipulate, and model using equations, which may include linear	 Essential Question How do patterns and functions help us describe data and physical phenomena and solve a variety of problems? 	Assessment • The Human Chain Skill Objectives
 quadratic and literal functions (formulas) and relations. graph linear equations. recognize functions by its equations and/or graphs. 	 Focus Questions How can we employ technology to create and interpret models and enhance student learning? What is slope and how is it related to the real world? What are the properties of a function and how can you recognize a function? 	 Skill Objectives Students will: identify when a relation is a function and use function notation. evaluate a function for a given value. make a table for a function and identify the domain and range. write a linear function in standard, slope-intercept and point-slope form and convert between forms. determine the slope and x and y intercepts of a linear function. explain the slope as a rate of change with units and the y intercept as an initial value within a real world context. model a real world situation with a constant rate of change using a linear functions. find the line of best fit given a set of data that appears to have a linear

	•	relationship. solve systems of equations by graphing, substitution and linear combination.

Unit 4 - Graphing, 7¹/₂ weeks top

<u>Standards</u>

Algebraic Reasoning: Patterns and Functions - Patterns and functional relationships can be represented and analyzed using a variety of strategies, tools, and technology.

1.1 Students should understand and describe patterns and functional relationships.

Core 1.1a Students should describe relationships and make generalizations about patterns and functions.

1.2 Students should represent and analyze quantitative relationships in a variety of ways.

Core 1.2a Students should represent and analyze linear and non-linear functions and relations symbolically and with tables and graphs.

Numerical and Proportional Reasoning - Quantitative relationships can be expressed numerically in multiple ways in order to make connections and simplify calculations using a variety of strategies, tools and technology.

2.2 Students should use numbers and their properties to compute flexibly and fluently, and to reasonably estimate measures and quantities.

Core 2.2a Students should develop strategies for computation and estimation using properties of number systems to solve problems.

2.2b Students should solve proportional reasoning problems.

Working with Data: Probability and Statistics - Data can be analyzed to make informed decisions using a variety of strategies, tools and technology. 4.1 Students should collect, organize and display data using appropriate statistical and graphical methods.

Core 4.1a Students should create the appropriate visual or graphical representation of real data.

<u>Unit Objectives</u>	Essential Questions	Assessment
Students will be able to:	• How do patterns and functions help us describe	Algebra Phone-tastic Giveaway
 create and interpret graphs with functions and relations (manually and with technology). create, solve and interpret systems of equations and inequalities graphically and algebraically. graph linear and quadratic equations. display, organize, and interpret data. make predictions based on graphs. 	 data and physical phenomena and solve a variety of problems? How are quantitative relationships represented by numbers? How can collecting, organizing and displaying data help us analyze information and make reasonable predictions and informed decisions? Focus Questions What is algebra and what role does it play in the world of mathematics? (i.e. Its importance as a foundation and tool in higher mathematics and the real world.) Given a real-world situation or set of data how can an algebraic model be created and applied? How can we employ technology to create and 	 Skill Objectives Students will: graph real numbers on a number line. graph simple and compound inequalities. graph solutions of absolute value equations and inequalities in one variable. graph ordered pairs and data using appropriate coordinate axes and labels. graph linear functions and inequalities. graph systems of linear functions. graph quadratic functions. make and use a scatter plot.

 interpret models and enhance student learning? How can data be organized and graphed in order to solve real-world situations? 	 make and use a stem and leaf plot to organize data. draw a box and whisker plot to organize and interpret real-life data.
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Unit 5 - Exponents and Radicals, 6 weeks top

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<u>Standards</u>		
Algebraic Reasoning: Patterns and Functions -	Patterns and functional relationships can be represented	and analyzed using a variety of strategies,
tools, and technology.		
1.1 Students should understand and describe pa	atterns and functional relationships.	
Core 1.1a Students should describe relation	onships and make generalizations about patterns and funct	ions.
Extended 1.1a Students should model real wor functions.	Id situations and make generalizations about mathematica	l relationships using a variety of patterns and
1.2 Students should represent and analyze quar	ntitative relationships in a variety of ways.	
Core 1.2a Students should represent and a	nalyze linear and non-linear functions and relations symbol	colically and with tables and graphs.
1.3 Students should use operations, properties,	and algebraic symbols to determine equivalence and so	olve problems.
Core 1.3a Students should manipulate equ	ations, inequalities, and functions to solve problems.	
Numerical and Proportional Reasoning - Quantalsimplify calculations using a variety of strategies2.1 Students should understand that a variety ofCore2.1a Students should extend the under 2.1b Students should interpret and re2.2 Students should use numbers and their propintCore2.2a Students should develop strategies 2.2b Students should solve proportion	tative relationships can be expressed numerically in multiplicative relationships can be expressed numerically in multiplications and technology. If numerical representations can be used to describe queerstanding of number to include integers, rational numbers expresent large sets of numbers with the aid of technology. In the present large sets of numbers with the aid of technology. It is for compute flexibly and fluently, and to reasonation is for computation and estimation using properties of numerical reasoning problems.	tiple ways in order to make connections and antitative relationships. a, and real numbers. ably estimate measures and quantities. nber systems to solve problems.
Unit Objectives	Essential Questions	Assessment
Students will be able to:	• How do patterns and functions help us describe	Classic Vs. New
• apply properties of, and perform	data and physical phenomena and solve a	
operations with, exponents and radicals.	variety of problems?	Skill Objectives
• multiply and Divide expressions with	• How are quantitative relationships represented	Students will:
exponents.	by numbers?	• define power, base and exponent.
• solve real-life problems with exponents		• use scientific notation when working
and radicals.	Focus Questions	with large and small numbers.
	• What is algebra and what role does it play in the	• evaluate power terms, with positive and
	world of mathematics? (i.e. Its importance as a	negative bases, with and without the
	foundation and tool in higher mathematics and	calculator.
	the real world.)	• apply properties of exponents to
	• Given a real-world situation or set of data how	simplify exponential expressions
	can an algebraic model be created and applied?	including positive, negative and zero
	• What are the properties of exponents and how	exponents.

are they applied to numeric expressions, algebraic expressions, and equations?	 evaluate expressions and equations using properties of exponents. write and use models for exponential growth and decay. use properties of radicals to express radicals in simplest form.
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Unit 6 – Polynomials, 3¹/₂ weeks top

<u>Standards</u>

Algebraic Reasoning: Patterns and Functions - Patterns and functional relationships can be represented and analyzed using a variety of strategies, tools, and technology.

1.1 Students should understand and describe patterns and functional relationships.

Core 1.1a Students should describe relationships and make generalizations about patterns and functions.

Extended 1.1a Students should model real world situations and make generalizations about mathematical relationships using a variety of patterns and functions.

1.2 Students should represent and analyze quantitative relationships in a variety of ways.

Core 1.2a Students should represent and analyze linear and non-linear functions and relations symbolically and with tables and graphs.

 Unit Objectives Students will be able to: perform operations on, manipulations with, and factoring of polynomials. do computations with polynomials (add, 	 Essential Question How do patterns and functions help us describe data and physical phenomena and solve a variety of problems? 	Assessment • Polynomial Crossword Puzzle Skill Objectives Students will:
 subtract, and multiply). factor polynomials with the purpose of solving equations. 	 What is algebra and what role does it play in the world of mathematics? (i.e. Its importance as a foundation and tool in higher mathematics and the real world.) What is a polynomial? How can you do computations and simplify a polynomial? How can a polynomial be factored? 	 identify coefficient, term, monomial, binomial, trinomial and polynomial. add, subtract and multiply polynomial expressions. factor polynomials by finding the greatest common factor. factor binomials that have a difference of two squares. factor any factorable trinomial with a leading coefficient of 1. solve quadratic equations by factoring, applying the quadratic formula, and graphing.