## **Mathematics**

# **Fairfield Public Schools**

## **GEOMETRY 21**



## **GEOMETRY 21**

#### **Critical Areas of Focus**

The fundamental purpose of the course in Geometry is to formalize and extend students' geometric experiences from the middle grades. Students explore more complex geometric situations and deepen their explanations of geometric relationships, moving towards formal mathematical arguments. Important differences exist between this Geometry course and the historical approach taken in Geometry classes. For example, transformations are emphasized early in this course. Close attention should be paid to the introductory content for the Geometry conceptual category found in the high school CCSS. The Mathematical Practice Standards apply throughout each course and, together with the content standards, prescribe that students experience mathematics as a coherent, useful, and logical subject that makes use of their ability to make sense of problem situations. The critical areas, organized into six topics, are as follows.

- 1. In previous grades, students were asked to draw triangles based on given measurements. They also have prior experience with rigid motions: translations, reflections, and rotations and have used these to develop notions about what it means for two objects to be congruent. In this unit, students establish triangle congruence criteria, based on analyses of rigid motions and formal constructions. They use triangle congruence as a familiar foundation for the development of formal proof. Students prove theorems—using a variety of formats—and solve problems about triangles, quadrilaterals, and other polygons. They apply reasoning to complete geometric constructions and explain why they work.
- 2. Students apply their earlier experience with dilations and proportional reasoning to build a formal understanding of similarity. They identify criteria for similarity of triangles, use similarity to solve problems, and apply similarity in right triangles to understand right triangle trigonometry, with particular attention to special right triangles and the Pythagorean theorem. Students develop the Laws of Sines and Cosines in order to find missing measures of general (not necessarily right) triangles, building on students' work with quadratic equations done in the first course. They are able to distinguish whether three given measures (angles or sides) define 0, 1, 2, or infinitely many triangles.
- 3. Students' experience with two-dimensional and three-dimensional objects is extended to include informal explanations of circumference, area and volume formulas. Additionally, students apply their knowledge of two-dimensional shapes to consider the shapes of cross-sections and the result of rotating a two-dimensional object about a line.
- 4. Building on their work with the Pythagorean theorem in 8th grade to find distances, students use a rectangular coordinate system to verify geometric relationships, including properties of special triangles and quadrilaterals and slopes of parallel and perpendicular lines, which relates back to work done in the first course. Students continue their study of quadratics by connecting the geometric and algebraic definitions of the parabola.
- 5. In this unit students prove basic theorems about circles, such as a tangent line is perpendicular to a radius, inscribed angle theorem, and theorems about chords, secants, and tangents dealing with segment lengths and angle measures. They study relationships among segments on chords, secants, and tangents as an application of similarity. In the Cartesian coordinate system, students use the distance formula to write the equation of a circle when given the radius and the coordinates of its center. Given an equation of a circle, they draw the graph in the coordinate plane, and apply techniques for solving quadratic equations, which relates back to work done in the first course, to determine intersections between lines and circles or parabolas and between two circles.

				Pac	cing	Guide					
1st M	Iarking Period		2nd Marking Po	ing Period 3rd Marking Period		4th Marking Period					
September	October N	ovember	December	January		February	March	April	May	June	
Unit 1  Modeling with Geometry &	Unit 2  Geometric Relation Properti		Unit 3  Coordinate Geometry	Unit 4 Similarity	ERM	Unit 5  Trigonometric Ratios	Unit 6  Rigid  Motions	Unit 7 <u>Circles and</u> <u>Conics</u>	Unit 8  Geometric  Measurement and Dimension	Unit 9  Capstone Project	T.
Definitions 2 weeks	10 week	S	2 weeks	2 weeks	MIDTERM	5 weeks	3 weeks	3 weeks	4 weeks	2 weeks	FINAL

Course Overview					
<ul> <li>Central Understandings</li> <li>Insights learned from exploring generalizations through the essential questions. (Students should understand that)</li> <li>Patterns and functional relationships can be represented and analyzed using a variety of strategies, tools, and technologies.</li> <li>Quantitative relationships can be expressed numerically in multiple ways in order to make connections and simplify calculations using a variety of strategies, tools, and technologies.</li> <li>Shapes and structures can be analyzed, visualized, measured, and transformed using a variety of strategies, tools, and technologies.</li> <li>Data can be analyzed to make informed decisions using a variety of strategies, tools, and technologies.</li> </ul>	<ul> <li>Essential Ouestions</li> <li>How do patterns and functions help us describe data and physical phenomena and solve a variety of problems?</li> <li>How are quantitative relationships represented by numbers?</li> <li>How do geometric relationships and measurements help us to solve problems and make sense of our world?</li> <li>How can collecting, organizing and displaying data help us analyze information and make reasonable and informed decision?</li> </ul>	Assessments  ■ Individual and district-wide Formative Assessments, Summative Assessments, and Projects.			

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Geometry	Standar	ds for	<b>Mathematical</b>	Practice
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The K-12 Standards for Mathematical Practice describe varieties of expertise that mathematics educators at all levels should seek to develop in their students. This page gives examples of what the practice standards look like at the specified grade level. Students are expected to:

	what the practice standards look like at the specified grade level. Students are expected to:
Standards	Explanations and Examples
1. Make sense	High school students start to examine problems by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens,
of problems	constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a
and persevere	solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They
in solving	monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or
them.	change the viewing window on their graphing calculator to get the information they need. By high school, students can explain correspondences between equations,
	verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. They check their answers
	to problems using different methods and continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems
	and identify correspondences between different approaches.
2. Reason	High school students seek to make sense of quantities and their relationships in problem situations. They abstract a given situation and represent it symbolically,
abstractly and	manipulate the representing symbols, and pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Students use
quantitatively.	quantitative reasoning to create coherent representations of the problem at hand; consider the units involved; attend to the meaning of quantities, not just how to compute
	them; and know and flexibly use different properties of operations and objects.
3. Construct	High school students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. By high school, a student might use
viable	geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. High school students making assumptions and
arguments	approximations to simplify a complicated ituation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and
and critique	map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw
the reasoning	conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model
of others.	if it has not served its purpose.
4. Model with	High school students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor,
mathematics.	a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. High school students should be sufficiently familiar with
	tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their
	limitations. For example, high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically
	using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying
	assumptions, explore consequences, and compare predictions with data. They are able to identify relevant external mathematical resources, such as digital content located
	on a website, and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.
5. Use	High school students try to communicate precisely to others by using clear definitions in discussion with others and in their own reasoning. They state the meaning of the
appropriate	symbols they choose, specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently,
tools	express numerical answers with a degree of precision appropriate for the problem context. By the time they reach high school they have learned to examine claims and
strategically.	make explicit use of definitions.
6. Attend to	By high school, students look closely to discern a pattern or structure. In the expression $x^2 + 9x + 14$ , older students can see the 14 as $2 \times 7$ and the 9 as $2 + 7$ . They
precision.	recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for
	an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For
	example, they can see $5 - 3(x - y)2$ as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers x and y.
	High school students use these patterns to create equivalent expressions, factor and solve equations, and compose functions, and transform figures.
7. Look for	High school students notice if calculations are repeated, and look both for general methods and for shortcuts. Noticing the regularity in the way terms cancel when
and make use	expanding $(x-1)(x+1)$ , $(x-1)(x^2+x+1)$ , and $(x-1)(x^3+x^2+x+1)$ might lead them to the general formula for the sum of a geometric series. As they work to solve a
of structure.	problem, derive formulas or make generalizations, high school students maintain oversight of the process, while attending to the details. They continually evaluate the
	reasonableness of their intermediate results.
8. Look for	By high school, students look closely to discern a pattern or structure. In the expression $x^2 + 9x + 14$ , older students can see the 14 as $2 \times 7$ and the 9 as $2 + 7$ . They
and express	recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for
regularity in	an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For
repeated	example, they can see $5 - 3(x - y)^2$ as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers x and y.
reasoning.	High school students use these patterns to create equivalent expressions, factor and solve equations, and compose functions, and transform figures.

## Unit 1 – Modeling with Geometry and Definitions, 2 weeks top

Students explore geometric ideas using key tools of geometry. This unit focuses on classical Euclidean compass and straightedge constructions, both by hand and in dynamic geometry environments. The goal is to both create constructions and explore why they work. The unit then considers other tools, such as string, paper folding, etc. As with the compass and straightedge constructions, it is important to both mechanically use these tools and to work toward mathematical explanations and justifications. In dynamic geometry environments, a key distinction is between drawing and constructing figure with particular characteristics. For example, if a rectangle is merely drawn to look like a rectangle, then it is easy to mess up the figure by dragging parts of the diagram. But a rectangle that is "constructed" as a rectangle will remain rectangular even when parts of the figure are dragged about. Building upon the informal experiences with basic geometric objects and relationships, the goal is to start increasing the precision of the definitions. The emphasis should be on the role of definitions and communicating mathematical explanations and arguments rather than on developing a deductive axiomatic system.

Big Ideas The central organizing ideas and underlying structures of mathematics	Essential Questions
<ul> <li>Understanding the language of geometry is essential to reasoning and making connections.</li> <li>Working with a variety of tools enhances understanding of geometric relationships.</li> <li>Geometric objects can have different definitions. Some are better than others, and their worth depends both on context and values.</li> <li>Definitions in geometry are of two distinct types: definition by genesis (how you can create the object) and definition by property (how you can characterize the object in terms of certain feature).</li> <li>Building definitions requires moving back and forth between verbal and the visual.</li> <li>Naming is not just about nomenclature: it draws attention to properties and objects of geometric interest.</li> </ul>	<ul> <li>How do geometric relationships and measurements help us to solve problems and make sense of our world?</li> <li>How do mathematical ideas interconnect and build on one another to produce a coherent whole?</li> <li>How does geometry model the physical world?</li> <li>How can the language of geometry be used to communicate mathematical ideas coherently and precisely?</li> <li>How does the language of geometry provide immediate experience with the physical world?</li> </ul>

#### **Common Core State Standards**

#### GEOMETRY

#### Congruence G-CO

#### Experiment with transformations in the plane.

#### G-CO 1

Know precise definitions of angle, eircle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, and plane, and distance along a line (length of a segment),

## Make geometric constructions.

#### G-CO 12

Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometric software, etc.). Copying a segment; copying an angle; bisecting a segment; bisecting an angle; constructing perpendicular lines, including the perpendicular bisector of a line segment and constructing a line parallel to a given line through a point not on the line.

## Expressing Geometric Properties with Equations

Use coordinates to prove simple geometric theorems algebraically.

## G-GPE 6

Find the point on a directed line segment between two given points that partitions the segment in a given ratio.

## Unit 2: Geometric Relationships and Properties, 10 weeks top

This unit brings together many of the "classic" theorems of geometry. The emphasis should be on the many roles of proof (a la Devilliers) and a focus on the mathematical practice of making viable arguments and critiquing the reasoning of others. Multiple representations (coordinates, sythemetic, and algebraic proofs of properties can be analyzed and compared). Once these logic concepts are built, the students will use these postulates and theorems to prove various geometric concepts and ideas with parallel lines, triangles, quadrilaterals, and polygons.

Big Ideas The central organizing ideas and underlying structures of mathematics	Essential Questions
<ul> <li>Geometric ideas are supported and derived using theorems, postulates, definitions, and properties.</li> <li>Formal proofs are created using a variety of formats.</li> <li>A written proof is the endpoint of the process of proving.</li> </ul>	<ul> <li>How do geometric relationships and measurements help us to solve problems and make sense of our world?</li> <li>How do mathematical ideas interconnect and build on one another to produce a coherent whole?</li> <li>How do reasoning and proofs provide the ideas and concepts that lead to an understanding of the deductive nature of geometry?</li> <li>How can various types of reasoning be used to make, investigate, and prove mathematical conjectures?</li> <li>How does the geometric principle of congruence in triangles apply to the real</li> </ul>
	<ul> <li>world?</li> <li>How do parallel lines, transversals, and related angles model the physical world?</li> <li>How does the geometric principle of congruence in triangles apply to the real world?</li> <li>How do triangles, their sides, angles, and special segments model the physical world?</li> <li>How does the set of quadrilaterals and their properties model the world around us?</li> </ul>

#### **Common Core State Standards**

#### GEOMETRY

Congruence G-CO

#### Experiment with transformations in the plane.

#### **G-CO 1**

Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, and plane, and distance along a line (length of a segment),

## Prove geometric theorems.

#### G-CO-Fairfield 1

Develop an understanding of conditionals, converses, and definitions and how they are used in proofs.

#### **G-CO9**

Prove theorems about lines and angles. Theorems include: vertical angles are congruent; when a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent; points on a perpendicular bisector of a line segment are exactly those equidistant from the segment's endpoints.

#### G-CO 10

Prove theorems about triangles. Theorems include: measures of interior angles of a triangle sum to 180°; base angles of isosceles triangles are congruent; the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length; the medians of a triangle meet at a point.

## G-CO 11

Prove theorems about parallelograms. Theorems include: opposite sides are congruent, opposite angles are congruent, the diagonals of a parallelogram bisect each other, and conversely, rectangles are parallelograms with congruent diagonals.

## Similarity, Right Triangles, and Trigonometry

Understand similarity in terms of similarity transformations.

## G-SRT 5

Use congruence and similarity criteria for triangles to solve problems and to prove relationships in geometric figures.

## **Unit 3 – Coordinate Geometry, 2 weeks top**

Making connections between geometric relationships and properties and algebraic expressions is a powerful mathematical tool. This unit provides opportunities to go back and forth between the algebra and geometry. It also builds upon the previous unit making connections between similarity and linearity, for example in f(x) = mx the slope m can be seen as a shape invariant of a right triangle and the x can viewed as the scale factor of the dilation centered at the origin.

Coordinates were introduced in grade 5:

Grade 5 Geometry 1: Graph points on the coordinate plane to solve real-world and mathematical problems.

Big Ideas  The central organizing ideas and underlying structures of mathematics	Essential Questions
The connection between algebra and geometry allows students to build geometric properties through algebraic approaches and thinking.	<ul> <li>How do patterns and functions help us describe data and physical phenomena and solve a variety of problems?</li> <li>How are quantitative relationships represented by numbers?</li> <li>How do geometric relationships and measurements help us to solve problems and make sense of our world?</li> <li>How does geometry model the physical world?</li> <li>How do mathematical ideas interconnect and build on one another to produce a coherent whole?</li> <li>How does algebra relate to geometry graphically?</li> </ul>

#### **Common Core State Standards**

#### GEOMETRY

Expressing Geometric Properties with Equations

Use coordinates to prove simple geometric theorems algebraically.

#### G-GPE 4

Use coordinates to prove simple geometric theorems algebraically. For example, prove or disprove that a figure defined by four given points in the coordinate plane is a rectangle; prove or disprove that the point  $(1, \sqrt{3})$  lies on the circle centered at the origin and containing the point (0,2).

#### G-GPE 5

Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point).

#### **G-GPE 7**

Use coordinates to compute perimeters of polygons and areas of triangles and rectangles, e.g., using the distance formula.\*

<sup>\*</sup> Denotes a modeling standard in the CCSS

## Unit 4 – Similarity, 2 weeks top

Similarity is defined using congruence and dilation. This geometric transformation definition of similarity and congruence is more general than comparing sides and angles. Define a similarity transformation as the composition of a dilation followed by congruence and prove that the meaning of similarity for triangles is the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides. The connection is made between similarity and linearity (why the graph of a linear function is a straight line).

This formalizes the Grade 8 standard 8.EE 6: Understand the connections between proportional relationships, lines, and linear equations.

Big Ideas The central organizing ideas and underlying structures of mathematics	Essential Questions
<ul> <li>Dilations and similarity are interconnected.</li> <li>Properties of similar figures are used to solve problems.</li> <li>Geometric awareness develops through practice in visualizing, diagramming, and constructing.</li> </ul>	<ul> <li>How do geometric relationships and measurements help us to solve problems and make sense of our world?</li> <li>How does geometry model the physical world?</li> <li>How do mathematical ideas interconnect and build on one another to produce a coherent whole?</li> <li>How are appropriate techniques, tools, and formulas used in geometry to determine measurements?</li> <li>How can a variety of appropriate strategies be applied in solving geometric problems?</li> <li>How is similarity used to measure indirectly and explore comparable objects?</li> </ul>

#### **Common Core State Standards**

#### GEOMETRY

Similarity, Right Triangles, and Trigonometry

Explore properties of similarity and prove theorems involving similarity.

#### G-SRT 4

Prove theorems about triangles. Theorems include: a line parallel to one side of a triangle divides the other two proportionally, and conversely; the Pythagorean Theorem proved using triangle similarity.

#### G-SRT 5

Use congruence and similarity criteria for triangles to solve problems and to prove relationships in geometric figures.

## **Unit 5 – Trigonometric Ratios, 5 weeks** top

This unit is the initial introduction of trigonometric ratios. The students will investigate the class of right triangles through the concept of similar triangles to develop the conceptual understanding of trigonometric ratios. From this conceptual understanding, the students will define the various relationships as sine = opposite/hypotenuse, cosine = adjacent/hypotenuse and tangent = opposite/adjacent. Once the students develop the concept of trigonometric ratios from right triangles, the development of the Law of Sines and Cosines allows students to solve problems with non-right triangles.

Big Ideas The central organizing ideas and underlying structures of mathematics	Essential Questions
<ul> <li>Trigonometric concepts build out of symmetry; these values are not dependent on the size of a triangle.</li> <li>Trigonometric ratios are well defined because the ratio of side lengths is equivalent in similar triangles.</li> </ul>	<ul> <li>How do geometric relationships and measurements help us to solve problems and make sense of our world?</li> <li>How does geometry model the physical world?</li> <li>How do mathematical ideas interconnect and build on one another to produce a coherent whole?</li> <li>How can a variety of appropriate strategies be applied in solving geometric problems?</li> <li>How is trigonometry used to understand the functional and aesthetic uses of right triangles?</li> <li>How do triangles, their sides, angles, and special segments model the physical world?</li> </ul>

#### **Common Core State Standards**

#### GEOMETRY

Similarity, Right Triangles, and Trigonometry

Define trigonometric ratios and solve problems involving right triangles.

#### G-SRT 6

Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles.

#### G-SRT 7

Explain and use the relationship between the sine and cosine of complementary angles.

#### G-SRT 8

Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.\*

#### G.SRT.9 (+)

Derive the formula  $A = \frac{1}{2}ab\sin(C)$  for the area of a triangle by drawing an auxiliary line from a vertex perpendicular to the opposite side.

#### G.SRT.10 (+)

Prove the Laws of Sines and Cosines and use them to solve problems.

#### G.SRT.11 (+)

Understand and apply the Law of Sines and the Law of Cosines to find unknown measurements in right and non-right triangles (e.g., surveying problems, resultant forces).

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#### G-SRT - Fairfield 1

Find missing sides of special right triangles (30-60-90 & 45-45-90) given two sides.

#### G-SRT – Fairfield 2

Find the area of regular polygons.

### Unit 6 – Rigid Motions, 3 weeks top

In this unit, the goal is to build on the students' study of rigid transformations. In Grade 8 rigid motions were explored, here they are defined more precisely and their properties explored. The concept of triangle congruence also is developed from the students understanding of transformational geometry.

Big Ideas The central organizing ideas and underlying structures of mathematics	Essential Questions	
Transformations assist students in developing knowledge of congruence.	<ul> <li>How do transformations provide a way of studying figures?</li> <li>How does the geometric principle of congruence in triangles apply to the real world?</li> </ul>	

#### Common Core State Standards

#### GEOMETRY

## Congruence G-CO

## Experiment with transformations in the plane.

#### G-CO<sub>2</sub>

Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch).

#### G-CO3

Given of a rectangle, parallelogram, trapezoid, or regular polygon, and describe the rotations and reflections that carry it onto itself.

#### **G-CO 4**

Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments.

#### **G-CO 5**

Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using, e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another.

#### **G-CO 6**

Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent.

#### **G-CO 7**

Use the definition of congruence in terms of rigid motions to show that two triangles are congruent if and only if corresponding pairs of sides and corresponding pairs of angles are congruent.

#### **G-CO8**

Explain how the criteria for triangle congruence (ASA, SAS, and SSS) follow from the definition of congruence in terms of rigid motions.

## Similarity, Right Triangles, and Trigonometry

## Understand similarity in terms of similarity transformations.

#### G-SRT 1

Verify experimentally the properties of dilations given by a center and a scale factor:

#### G-SRT 1a

A dilation takes a line not passing through the center of the dilation to a parallel line, and leaves a line passing through the center unchanged.

#### G-SRT 1b

The dilation of a line segment is longer or shorter in the ratio given by the scale factor.

## G-SRT 2

Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides.

## G-SRT 3

Use the properties of similarity transformations to establish the AA criterion for two triangles to be similar

## Unit 7 – Circles and Conics, 3 weeks top

This unit includes key results about circles, treated both synthetically, with attention to constructions, and analytically. Conic sections can arise out of mechanical constructions (e.g. loop of string around two fixed nails to produce an ellipse, paper folding to produce a parabola). Applications can be considered such as elliptic orbits, parabolic motion of projectiles.

The central organizing ideas and underlying structures of mathematics	Essential Questions
Circles have intrinsic properties that produce different geometric concepts.	<ul> <li>How do geometric relationships and measurements help us to solve problems and make sense of our world?</li> <li>How can collecting, organizing and displaying data help us analyze information and make reasonable predictions and informed decisions?</li> </ul>
	<ul> <li>and make reasonable predictions and informed decisions?</li> <li>How does geometry model the physical world?</li> <li>How do mathematical ideas interconnect and build on one another to produce a coherent whole?</li> <li>How can a variety of appropriate strategies be applied in solving geometric problems?</li> <li>How do circles and their parts relate to the physical world?</li> </ul>

#### **Common Core State Standards**

#### GEOMETRY

Congruence G-CO

Make geometric constructions.

G-CO 13

Construct an equilateral triangle, a square, and a regular hexagon inscribed in a circle.

#### Circles

### Understand and apply theorems about circles.

G-C 1

Prove that all circles are similar.

G-C 2

Identify and describe relationships among inscribed angles, radii, and chords, and find the distance around a circular arc. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle.

G-C 5

Derive using similarity the fact that the length of the arc intercepted by an angle is proportional to the radius, and define the radian measure of the angle as the constant of proportionality; derive the formula for the area of a sector.

G-C 3

Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle.

G.C.4(+)

Construct a tangent line from a point outside a given circle to the circle.

## Expressing Geometric Properties with Equations

Translate between the geometric description and the equation for a conic section.

## G-GPE 1

Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation.

## G-GPE 2

Derive the equation of a parabola given a focus and directrix.

(+) denotes a standard in Geometry 21 and not in Geometry 22

#### Unit 8 – Geometric Measurement and Dimension, 4 weeks top

This unit should treat geometric measurement more comprehensively and make connections and explain the various volume formulae with attention to the structure of the algebraic expressions. Moving between 2 and 3 dimensions such as via slicing and rotation, and establishing phenomena as fundamental contexts for quadratic relationships and volume phenomena as fundamental contexts for cubic relationships.

This builds on the 7th grade geometry standard: 7G-G Solve real-life and mathematical problems involving angle measure, area, surface area, and volume.

Big Ideas The central organizing ideas and underlying structures of mathematics	Essential Questions
<ul> <li>Area is based upon the concept of two-dimensional space, which covers the outside of a three-dimensional object.</li> <li>Volume is the space contained in a three-dimensional object.</li> </ul>	<ul> <li>How do geometric relationships and measurements help us to solve problems and make sense of our world?</li> <li>How does geometry model the physical world?</li> <li>How do mathematical ideas interconnect and build on one another to produce a coherent whole?</li> <li>How can a variety of appropriate strategies be applied in solving geometric problems?</li> <li>How do the calculations and concepts of area and volume relate to two and three-dimensional objects?</li> </ul>

#### **Common Core State Standards**

#### GEOMETRY

Geometric Measurement and Dimension

Explain volume formulas and use them to solve problems.

#### G-GMD 1

Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a prism, cylinder, pyramid, and cone. Use dissection arguments, Cavalieri's principle, and informal limit arguments.

#### G-GMD 3

Use volume formulas for (prisms), cylinders, pyramids, cones, and spheres to solve problems.

#### **G-GMD-Fairfield 1**

Calculate the missing side, surface area, and volume using linear, area, and volume ratios respectively.

## Visualize relationships between two-dimensional and three-dimensional objects.

#### **G-GMD 4**

Identify the shapes of two-dimensional cross-sections of three-dimensional objects, and identify three-dimensional objects generated by rotations of two-dimensional objects.

## Unit 9 – Capstone Geometric Modeling Project, 2 weeks top

The purpose of this unit is to provide closure to the year by wrapping up the big ideas that students learned and synthesize a project.

The purpose of this time is to provide crosure to the year of waapping up the org racus that stadents retained that synthesize a project.	
Big Ideas The central organizing ideas and underlying structures of mathematics	<b>Essential Questions</b>
<ul> <li>Geometry and other mathematical ideas allow individuals to solve open- ended and complex problems.</li> </ul>	How can geometric concepts be used to help solve problems?

#### **Common Core State Standards**

## GEOMETRY

Modeling with Geometry

Apply geometric concepts in modeling situations.

**G-MG 1** 

Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).\*

**G-MG 2** 

Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot).\*

**G-MG 3** 

Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).\*

<sup>\*</sup> denotes a modeling standard in the CCSS